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NOIDA INSTITUTE OF ENGINEERING AND TECHNOLOGY, GREATER NOIDA

(An Autonomous Institute Affiliated to AKTU, Lucknow)

B.Tech.

SEM: II - THEORY EXAMINATION (2020 - 2021)

Subject: Engineering Mathematics-II

Time: 03:00 Hours

Max. Marks: 100

General Instructions:

- All questions are compulsory. It comprises of three Sections A, B and C.
- Section A - Question No- 1 is objective type question carrying 1 mark each & Question No- 2 is Very short type questions carrying 2 marks each.
- Section B - Question No- 3 is Long answer type - 1 questions carrying 6 marks each.
- Section C - Question No- 4 to 8 are Long answer type -2 questions carrying 10 marks each.

SECTION A

20

1. Attempt all parts:-

- 1-a. The P.I. of the differential equation $(D^2 + 1)y = \sin x$ CO 1 1
1. $(-x/2) \cos x$
 2. $(x/2) \cos x$
 3. $(x/2) \sin x$
 4. $(x/4) \sin x$
- 1-b. The value for $\frac{1}{D-2} \sin 2x$ CO 1 1
1. $e^{2x} \int e^{2x} \sin 2x dx$
 2. $e^{2x} \int e^{-2x} \sin 2x dx$
 3. $e^{-2x} \int e^{2x} \sin 2x dx$
 4. None of these
- 1-c. The Series $1 + \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{3}} + \frac{1}{\sqrt{4}} + \frac{1}{\sqrt{5}} + \dots$ is (CO2) 1
1. convergent
 2. oscillatory
 3. divergent
 4. none of these
- 1-d. The coefficient a_0 in a Fourier series for the function $f(x) = x + x^3$ in the interval $-\pi < x < \pi$ is (CO2) 1
1. π
 2. 2π

3. 0

4. none of these

1-e. Laplace Transform of the function $F(t) = \cos h 3t$ is CO 3 1

1. $\frac{s}{s^2-9}$

2. $\frac{3}{s^2+9}$

3. $\frac{1}{s^2+9}$

4. $\frac{s}{s^2+9}$

1-f. Inverse Laplace of the function $f(s) = \left[\frac{-5}{s^2+s-6} \right]$ is 1

CO 3

1. $e^{3t} - e^{2t}$

2. $e^{3t} + e^{2t}$

3. $e^{3t} + e^t$

4. None of these

1 Find the unit normal at the surface $z = x^2 + y^2$ at the point (1,2,5) is (CO4) 1

1. $2x + 4y$

2. $2x \hat{i} + 4y \hat{j}$

3. $\frac{-2x \hat{i} - 4y \hat{j} + \hat{k}}{\sqrt{21}}$

4. None of these

1 If $\text{div } \vec{F} = 0$ every where in some region R of space, then \vec{V} is called (CO4) 1

1. Irrotational

2. Rotational

3. Solenoidal

4. None of these

1-i. Find the mean proportional between given two numbers that is 64 and 49 ? (CO5) 1

1. 45

2. 52

3. 54

4. 56

1-j. Find the simple interest on Rs 500 for 5 years at 10% per annum. (CO5) 1

1. Rs 500

2. Rs 125

3. Rs 250

4. Rs 350

2. Attempt all parts:-

- 2.a. Find the complementary function of the second order linear differential equation $x^2y'' + xy' + y = \log x^2$ CO 1 2
- 2.b. Write the statement of Rabbe's test for the series $\sum u_n$ CO-2 2
- 2.c. Find Laplace transform of the function $F(t) = \frac{\cos at - \cos bt}{t}$. CO 3 2
- 2.d. If $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$, then show that $\text{grad} (r) = \frac{\vec{r}}{r}$ (CO4) 2
- 2.e. After 2 years, the age of Karthi is 2 times the present age of Silambu. Preethi is 8 years elder than Silambu. Find the present age of Karthi, if the present age of Preethi is 23 years? (CO5) 2

SECTION B

30

3. Answer any five of the following-

- 3-a. Solve: $\frac{d^2y}{dx^2} + 2\frac{dy}{dx} + y = x^2e^{-x} \cos x$. CO 1 6
- 3-b. Solve the differential equation $xy'' - y' + (1-x)y = x^2e^{-x}$, given that $y = e^x$ is a part of CF. CO 1 6
- 3-c. Test the convergence of the series $\sum_{n=1}^{\infty} \left[(n^4 + 1)^{\frac{1}{4}} - n \right]$ CO-2 6
- 3-d. Test the convergence of the series, $\frac{x}{1.2} + \frac{x^2}{2.3} + \frac{x^3}{3.4} + \frac{x^4}{4.5} + \dots$ CO-2 6
- 3-e. Find the Laplace Transform of the function $\int_0^t \frac{e^{-4u} \sin 3u}{u} du$. CO 3 6

3-f. Show that $\vec{F} = (\sin y + z)\hat{i} + (x \cos y - z)\hat{j} + (x - y)\hat{k}$, is irrotational. Also find the Scalar potential. (CO4) 6

3-g. (i) The respective ratio of the present ages of a mother and daughter is 7: 1. Four years ago the

respective ratio of their ages was 19:1. What will be the mother's age four years from now?

(ii) The ages of Aarzu and Arnav are in the ratio of 11:13 respectively. After 7 years the ratio

of their ages will be 20:23. What is the difference in years between their ages? (CO5)

SECTION C

50

4. Answer any one of the following-

4-a. Solve the following differential equation by changing the independent variable 10

$$\frac{d^2y}{dx^2} - \frac{1}{x} \frac{dy}{dx} + 4x^2y = x^4. \quad \text{CO 1}$$

4-b. Solve $\frac{dx}{dt} + 2x - 3y = t$, $\frac{dy}{dt} - 3x + 2y = e^{2t}$. 10

CO 1

5. Answer any one of the following-

5-a. Obtain the Fourier series for the function $f(x) = \frac{1}{4}(\pi - x)^2$ in the interval $0 \leq x \leq 2\pi$. CO-2 10

Hence obtain the following relations:

$$(i) \frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \frac{1}{4^2} + \dots = \frac{\pi^2}{6} \quad (ii) \frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots = \frac{\pi^2}{12}$$

$$(iii) \frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots = \frac{\pi^2}{8}$$

5-b. Obtain the Fourier series for the function $f(x) = \begin{cases} 0, & -\pi \leq x \leq 0 \\ \sin x, & 0 \leq x \leq \pi \end{cases}$. (CO2) 10

$$\text{Hence show that } \frac{1}{1.3} + \frac{1}{3.5} + \frac{1}{5.7} + \dots = \frac{1}{2}$$

6. Answer any one of the following-

6 Find the Laplace transform of the rectified semi wave function defined by 10

$$f(t) = \begin{cases} \sin \omega t & 0 \leq t < \frac{\pi}{\omega} \\ 0 & \frac{\pi}{\omega} \leq t < \frac{2\pi}{\omega} \end{cases} \quad \text{CO 3}$$

6 Solve the following differential equation by using Laplace transformation 10

$$\frac{d^2x}{dt^2} + 2\frac{dx}{dt} + x = t e^{-t}, \text{ Given that } x(0) = 1, x'(0) = 2 \quad \text{CO 3}$$

7. Answer any one of the following-

7-a. Evaluate $\oint_C \vec{F} \cdot d\vec{r}$, by stokes theorem, where $\vec{F} = y^2\hat{i} + x^2\hat{j} - (x+z)\hat{k}$ and C is the boundary of the triangle with vertices $(0,0,0)$, $(1,0,0)$, and $(0,1,0)$. 10

7-b. Find the directional derivative of \vec{V}^2 where $\vec{V} = xy^2\hat{i} + zy^2\hat{j} + xz^2\hat{k}$ at the point $(2,0,3)$ in the direction of the outward normal to the surface $x^2 + y^2 + z^2 = 14$. 10

8. Answer any one of the following-

8-a. (i) Amit started a business by investing ₹ 30,000. Rahul joined the business after some time and invested ₹ 20,000. At the end of the year, profit was divided in the ratio of 2: 1. After how many months did Rahul join the business? 10

(ii) The monthly income of Komal and Asha are in the ratio of 4: 3. Their monthly expenses are in the ratio of 3: 2. However both saves ₹ 600 per month. What is their total monthly income? (CO5)

8-b. (i) I was facing East from where I turned to my left and walked 12 feet then I turned towards right and walked 6 feet. After that I walked 6 feet in South direction and at last walked 6 feet in the West. Then, in which direction am I standing from the original point? 10

(ii) Radha left her home in the morning and walked towards the East for 4 km and then took a 90° anticlockwise turn and walked for another 3 km to reach her school. On the same day in the morning, her brother Raman left the same house and walked towards the South for 6 km and took a right turn and walked for 8 km to reach his college. What is the shortest distance between Radha's school and Raman's college? (CO5)