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NOIDA INSTITUTE OF ENGINEERING AND TECHNOLOGY, GREATER NOIDA

(An Autonomous Institute Affiliated to AKTU, Lucknow)

B.Tech.

SEM: III - CARRY OVER THEORY EXAMINATION - SEPTEMBER 2022

Subject: Discrete Structures

Time: 3 Hours

Max. Marks: 100

General Instructions:

1. The question paper comprises three sections, A, B, and C. You are expected to answer them as directed.
2. Section A - Question No- 1 is 1 marker & Question No- 2 carries 2 mark each.
3. Section B - Question No-3 is based on external choice carrying 6 marks each.
4. Section C - Questions No. 4-8 are within unit choice questions carrying 10 marks each.
5. No sheet should be left blank. Any written material after a blank sheet will not be evaluated/checked.

SECTION A

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1. Attempt all parts:-

- 1-a. What is the Cartesian product of $A = \{1, 2\}$ and $B = \{a, b\}$? (CO1) 1
- (a) $\{(1, a), (1, b), (2, a), (b, b)\}$
- (b) $\{(1, 1), (2, 2), (a, a), (b, b)\}$
- (c) $\{(1, a), (2, a), (1, b), (2, b)\}$
- (d) $\{(1, 1), (a, a), (2, a), (1, b)\}$
- 1-b. What is the cardinality of the set of odd positive integers less than 10? (CO 1) 1
- (a) 10
- (b) 5
- (c) 3
- (d) 20
- 1-c. Let a binary operation '*' be defined on a set A. The operation will be commutative if _____ (CO 2) 1
- (a) $a*b=b*a$
- (b) $(a*b)*c=a*(b*c)$
- (c) $(b \circ c)*a=(b*a) \circ (c*a)$

(d) $a*b=a$

- 1-d. A subgroup has the properties of _____. (CO 2) 1
- (a) Closure, associative
 - (b) Commutative, associative, closure
 - (c) Inverse, identity, associative
 - (d) Closure, associative, Identity, Inverse
- 1-e. A Poset in which every pair of elements has both a least upper bound and a greatest lower bound is termed as _____. (CO3) 1
- (a) lattice
 - (b) sublattice
 - (c) trail
 - (d) walk
- 1-f. The relation \leq is a partial order if it is _____. (CO 3) 1
- (a) reflexive, antisymmetric and transitive
 - (b) reflexive, symmetric
 - (c) asymmetric, transitive
 - (d) irreflexive and transitive
- 1-g. Let P: If Sahil bowls, Saurabh hits a century.; Q: If Raju bowls, Sahil gets out on first ball. Now if P is true and Q is false then which of the following can be true? (CO4) 1
- (a) Raju bowled and Sahil got out on first ball
 - (b) Raju did not bowled
 - (c) Sahil bowled and Saurabh hits a century
 - (d) Sahil bowled and Saurabh got out
- 1-h. $(p \rightarrow q) \wedge (p \rightarrow r)$ is logically equivalent to _____. (CO 4) 1
- (a) $p \rightarrow (q \wedge r)$
 - (b) $p \rightarrow (q \vee r)$
 - (c) $p \wedge (q \vee r)$
 - (d) $p \vee (q \wedge r)$
- 1-i. Another name for the directed graph is (CO5) 1
- (a) Direct graph
 - (b) Bigraph

(c) Dir-graph

(d) Digraph

- 1-j. The degree of any vertex of graph is. (CO 5) 1
- (a) The number of edges incident with vertex
 - (b) Number of vertex in a graph
 - (c) Number of vertices adjacent to that vertex
 - (d) Number of edges in a graph

2. Attempt all parts:-

- 2.a. Name three operations possible on Sets. (CO1) 2
- 2.b. Show that $G = \{1, -1\}$ is an abelian group under multiplication. (CO 2) 2
- 2.c. Define POSET with suitable example. (CO 3) 2
- 2.d. Use truth tables to verify the associative laws:
 $(p \vee q) \vee r \equiv p \vee (q \vee r)$. (CO 4) 2
- 2.e. Define isomorphism between two graphs. (CO 5) 2

SECTION B

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3. Answer any five of the following:-

- 3-a. Let f and g be the functions from the set of integers to the set of integers defined by $f(x) = 2x + 3$ and $g(x) = 3x + 2$. What is the composition of f and g ? What is the composition of g and f ? (CO 1) 6
- 3-b. What is recurrence relation. Also define order and degree of recurrence relation. (CO1) 6
- 3-c. Show that $G = \{1, w, w^2\}$ is an abelian group under multiplication. Where $1, w, w^2$ are cube roots of unity. (CO2) 6
- 3-d. The set $G = \{0,1,2,3,4,5\}$ is a group with respect to addition modulo 6. (CO2) 6
- 3.e. Explain Modular lattice, distribute lattice and bounded lattice with example and diagram (CO3) 6
- 3.f. What is a tautology, contradiction and contingency? Show that $(P \vee Q) \wedge (\neg P \vee R) \rightarrow (Q \vee R)$ is tautology, contradiction or contingency. (CO4) 6
- 3.g. Draw the graph : i) Graph having Euler's circuit and Hamiltonian circuit both. ii) Graph having Euler's circuit but not Hamiltonian circuit. (CO5) 6

SECTION C

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4. Answer any one of the following:-

- 4-a. What is Ordered set and Ordered pairs. If set A have 5 numbers of elements and set B have 4 10

number of elements then what will be the cardinality of 'A X B', give example. (CO1)

4-b. How matrices is helpful to find composition of relation. 10

Let $A = \{2, 3, 4, 5\}$. Consider the relation R and S on A defined by

$R = \{(2, 2), (2, 3), (2, 4), (2, 5), (3, 4), (3, 5), (4, 5), (5, 3)\}$

$S = \{(2, 3), (2, 5), (3, 4), (3, 5), (4, 2), (4, 3), (4, 5), (5, 2), (5, 5)\}$. Find (i) $R \circ S$ (ii) $S \circ R$
(CO1)

5. Answer any one of the following:-

5-a. Explain Group with example. The set $G = \{1,2,3,4,5,6\}$ is a group with respect to multiplication modulo 7. (CO2) 10

5-b. Let G be a group. Prove that every subgroup H of G of index 2 is a normal subgroup. (CO2) 10

6. Answer any one of the following:-

6-a. Answer these questions for the poset($\{3, 5, 9, 15,24, 45\}, \cdot$). (CO3) 10

i. Find the minimal elements.

ii. Is there a greatest element?

iii. Is there a least element?

iv. Find all upper bounds of $\{3, 5\}$.

6-b. find the product of sum expansion of each of the following 10

(a). $f(x,y,z)=(x+z)y$ (b). $F(x,y,z)= x$ (CO3)

7. Answer any one of the following:-

7-a. Use the quantifiers to express following statements: (CO4) 10

1. there is a student in the class who can speak Hindi.

2.every student in this class knows how to drive a car.

3.some student in this class knows has visited Alaska but not visited Hawaii.

4.all students in this class have learned at least one programming language.

7-b. Show that each of these conditional statements is a tautology by using truth tables. (CO4) 10

a) $(p \wedge q) \rightarrow p$,

b) $p \rightarrow (p \vee q)$,

c) $\neg p \rightarrow (p \rightarrow q)$,

d) $(p \wedge q) \rightarrow (p \rightarrow q)$,

e) $\neg(p \rightarrow q) \rightarrow p$

f) $\neg(p \rightarrow q) \rightarrow \neg q$

8. Answer any one of the following:-

- 8-a. Show that there does not exist a graph with 5 vertices with degrees 1, 3, 4, 2, 3 respectively. 10
Also explain Define Graph coloring. What is its application? (CO5)
- 8-b. Construct the binary tree using following in-order and post-order traversal. (CO5) 10
In-order : DBMINEAFCJGK
Post-order : ABDEIMNCFGJK
Also Find the Pre-order of the constructed Binary Tree.